

## **Final study guide**

### Cumulative Final

**The final is cumulative. Review the topics from Test 1 and Test 2 and the information below.**

### Topics from after Test 1 and Test 2

- Computation: Examples on 11/19 slide 7 where we classified the abelian groups of size 180 and 539,539 up to isomorphism.
- Review these HW problems:
  - 4.4 # 2
  - 4.5 # 5, 13, 30
  - 5.2 # A, B
  - 5.4 # A
- Look at the problems from class where we classified a group of a certain size.
  - Example from 11/14 slides 2,3,4 – A group of size 15 is cyclic.
  - Example from 11/14 slides 5,6 – A group of size 255 is abelian.
  - Example from 11/21 slides 9,10,11 – Classify the groups of size 45 up to isomorphism.
- Know these proofs from class. One of them will be on the final.
  - Lecture 10/15 slide 6 – Let  $G$  be a group of size  $p^\alpha$  where  $p$  is prime and  $\alpha \geq 1$ , then  $|Z(G)| > 1$ .
  - Lecture 10/15 slide 8 – Let  $G$  be a group of size  $p^2$  where  $p$  is prime, then  $G$  is abelian.
  - Lecture 11/7 last slide – The theorem about  $n_p$  with two parts.
  - Lecture 11/21 slide 3 –  $G$  is abelian iff  $G' = \{1\}$
  - Lecture 11/21 slides 4,5,6,7,8 – Theorem with 3 parts about  $G'$ .