

```

In[95]:= (* ****)
(* Functions      *)
(****)

(* returns a list of all the
 Gaussian Integers with norm equal to n *)
normSolver[n_] := Module[{a, b, sqrtN, answerlist},
  sqrtN = Sqrt[n];
  answerlist = {};
  For[a = Floor[-sqrtN], a ≤ sqrtN, a++,
    For[b = Floor[-sqrtN], b ≤ sqrtN, b++,
      If[Equal[n, a*a + b*b],
        answerlist = Append[answerlist, a + b*I];
      ];
    ];
  ];
  Return[answerlist];
];

(* If z and w are Gaussian integers,
this module returns True if z divides w, otherwise
it returns False *)
gaussianDivides[z_, w_] := Module[{quotient},
  quotient = Simplify[w/z];
  If[IntegerQ[Re[quotient]] && IntegerQ[Im[quotient]],
    Return[True];
  ];
  Return[False];
];

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(* Given a Gaussian integer z,
this function returns a list of all
the Gaussian integers that divide z *)
findAllDivisors[z_] := Module[{answerList,
    zNorm, normDivisors, possibleDivisorList, i},

    possibleDivisorList = {};
    answerList = {};

    (* get the norm of z
       and then find all possible divisors of
       that norm *)
    zNorm = Norm[z]^2;
    normDivisors = Divisors[zNorm];

    (* find all w that could possibly divide z *)
    For[i = 1, i ≤ Length[normDivisors], i++,
        possibleDivisorList = Join[possibleDivisorList,
            normSolver[normDivisors[[i]]]];
    ];

    (* Now check which ones actually do divide w *)
    For[i = 1, i ≤ Length[possibleDivisorList], i++,
        If[gaussianDivides[possibleDivisorList[[i]], z],
            answerList =
                Append[answerList, possibleDivisorList[[i]]];
        ];
    ];

    Return[answerList];
}
```

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];

(* returns true if z is a prime in the
Gaussian Integers.  returns False otherwise *)
isPrime[z_] := Module[{},
  If[Equal[Length[findAllDivisors[z]], 8],
    Return[True];
  ];
  Return[False];
];

(*****)
(* Test some
Gaussian integers *)
(*****)
*****)
```

```
In[99]:= z = 2;
answer = findAllDivisors[z];
Print["Here are the divisors of ",
z, " : ", answer];
Print["There are ", Length[answer],
" divisors of ", z, "."];
If[isPrime[z],
Print[z, " is prime."]
,
Print[z, " is not prime."]
];
Here are the divisors of 2 : {-1, -1, 1, 1,
-1 - 1, -1 + 1, 1 - 1, 1 + 1, -2, -2 1, 2 1, 2}
There are 12 divisors of 2.
2 is not prime.

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```
In[104]:= z = 3;
answer = findAllDivisors[z];
Print["Here are the divisors of ",
z, " : ", answer];
Print["There are ", Length[answer],
" divisors of ", z, "."];
If[isPrime[z],
Print[z, " is prime."]
,
Print[z, " is not prime."]
];
```

Here are the divisors of 3  
: {-1, - $\frac{1}{3}$ ,  $\frac{1}{3}$ , 1, -3, -3  $\frac{1}{3}$ , 3  $\frac{1}{3}$ , 3}

There are 8 divisors of 3.

3 is prime.

(\*\*\*\*\*  
\*\*\*\*\*)

```
In[109]:= z = 5;  
answer = findAllDivisors[z];  
Print["Here are the divisors of ",  
z, " : ", answer];  
Print["There are ", Length[answer],  
" divisors of ", z, "."];  
If[isPrime[z],  
Print[z, " is prime."]  
,Print[z, " is not prime."]  
];
```

Here are the divisors of 5 :

```
{-1, -1, 1, 1, -2 - 1, -2 + 1, -1 - 2 1, -1 + 2 1,  
1 - 2 1, 1 + 2 1, 2 - 1, 2 + 1, -5, -5 1, 5 1, 5}
```

There are 16 divisors of 5.

5 is not prime.

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( *****  
***** )
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```
In[119]:= z = 10;
answer = findAllDivisors[z];
Print["Here are the divisors of ",
z, " : ", answer];
Print["There are ", Length[answer],
" divisors of ", z, "."];
If[isPrime[z],
Print[z, " is prime."]
,
Print[z, " is not prime."]
];
```

Here are the divisors of 10 :

```
{-1, -1 $\frac{i}{2}$ ,  $\frac{i}{2}$ , 1, -1 -  $\frac{i}{2}$ , -1 +  $\frac{i}{2}$ , 1 -  $\frac{i}{2}$ , 1 +  $\frac{i}{2}$ ,
-2, -2 $\frac{i}{2}$ , 2 $\frac{i}{2}$ , 2, -2 -  $\frac{i}{2}$ , -2 +  $\frac{i}{2}$ , -1 - 2 $\frac{i}{2}$ ,
-1 + 2 $\frac{i}{2}$ , 1 - 2 $\frac{i}{2}$ , 1 + 2 $\frac{i}{2}$ , 2 -  $\frac{i}{2}$ , 2 +  $\frac{i}{2}$ ,
-3 -  $\frac{i}{2}$ , -3 +  $\frac{i}{2}$ , -1 - 3 $\frac{i}{2}$ , -1 + 3 $\frac{i}{2}$ , 1 - 3 $\frac{i}{2}$ ,
1 + 3 $\frac{i}{2}$ , 3 -  $\frac{i}{2}$ , 3 +  $\frac{i}{2}$ , -4 - 2 $\frac{i}{2}$ , -4 + 2 $\frac{i}{2}$ ,
-2 - 4 $\frac{i}{2}$ , -2 + 4 $\frac{i}{2}$ , 2 - 4 $\frac{i}{2}$ , 2 + 4 $\frac{i}{2}$ , 4 - 2 $\frac{i}{2}$ ,
4 + 2 $\frac{i}{2}$ , -5, -5 $\frac{i}{2}$ , 5 $\frac{i}{2}$ , 5, -5 - 5 $\frac{i}{2}$ , -5 + 5 $\frac{i}{2}$ ,
5 - 5 $\frac{i}{2}$ , 5 + 5 $\frac{i}{2}$ , -10, -10 $\frac{i}{2}$ , 10 $\frac{i}{2}$ , 10}
```

There are 48 divisors of 10.

10 is not prime.

```
(*****  
***** )  
  
In[134]:= z = 11;  
answer = findAllDivisors[z];  
Print["Here are the divisors of ",  
      z, " : ", answer];  
Print["There are ", Length[answer],  
      " divisors of ", z, "."];  
If[isPrime[z],  
  Print[z, " is prime."]  
,  
  Print[z, " is not prime."]  
];
```

Here are the divisors of 11 :

{-1, - $\frac{1}{2}$ ,  $\frac{1}{2}$ , 1, -11, -11  $\frac{1}{2}$ , 11  $\frac{1}{2}$ , 11}

There are 8 divisors of 11.

11 is prime.

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(*****  
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In[124]:= z = 13;  
answer = findAllDivisors[z];  
Print["Here are the divisors of ",  
      z, " : ", answer];  
Print["There are ", Length[answer],  
      " divisors of ", z, "."];  
If[isPrime[z],  
  Print[z, " is prime."]  
  ,  
  Print[z, " is not prime."]  
];
```

Here are the divisors of 13

```
: {-1, -13, 13, 1, -3 - 2 I, -3 + 2 I,  
-2 - 3 I, -2 + 3 I, 2 - 3 I, 2 + 3 I,  
3 - 2 I, 3 + 2 I, -13, -13 I, 13 I, 13}
```

There are 16 divisors of 13.

13 is not prime.

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(*****  
*****)
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```
In[129]:= z = 100;
answer = findAllDivisors[z];
Print["Here are the divisors of ",
z, " : ", answer];
Print["There are ", Length[answer],
" divisors of ", z, "."];
If[isPrime[z],
Print[z, " is prime."]
,
Print[z, " is not prime."]
];
```

Here are the divisors of 100 :

```
{-1, -1, 1, 1, -1 - I, -1 + I, 1 - I, 1 + I, -2,
-2 I, 2 I, 2, -2 - I, -2 + I, -1 - 2 I, -1 + 2 I,
1 - 2 I, 1 + 2 I, 2 - I, 2 + I, -2 - 2 I, -2 + 2 I,
2 - 2 I, 2 + 2 I, -3 - I, -3 + I, -1 - 3 I,
-1 + 3 I, 1 - 3 I, 1 + 3 I, 3 - I, 3 + I, -4, -4 I,
4 I, 4, -4 - 2 I, -4 + 2 I, -2 - 4 I, -2 + 4 I,
2 - 4 I, 2 + 4 I, 4 - 2 I, 4 + 2 I, -5, -4 - 3 I,
-4 + 3 I, -3 - 4 I, -3 + 4 I, -5 I, 5 I, 3 - 4 I,
3 + 4 I, 4 - 3 I, 4 + 3 I, 5, -6 - 2 I, -6 + 2 I,
-2 - 6 I, -2 + 6 I, 2 - 6 I, 2 + 6 I, 6 - 2 I,
6 + 2 I, -7 - I, -7 + I, -5 - 5 I, -5 + 5 I,
```

$-1 - 7 \mathbb{i}, -1 + 7 \mathbb{i}, 1 - 7 \mathbb{i}, 1 + 7 \mathbb{i}, 5 - 5 \mathbb{i},$   
 $5 + 5 \mathbb{i}, 7 - \mathbb{i}, 7 + \mathbb{i}, -8 - 4 \mathbb{i}, -8 + 4 \mathbb{i}, -4 - 8 \mathbb{i},$   
 $-4 + 8 \mathbb{i}, 4 - 8 \mathbb{i}, 4 + 8 \mathbb{i}, 8 - 4 \mathbb{i}, 8 + 4 \mathbb{i},$   
 $-10, -8 - 6 \mathbb{i}, -8 + 6 \mathbb{i}, -6 - 8 \mathbb{i}, -6 + 8 \mathbb{i},$   
 $-10 \mathbb{i}, 10 \mathbb{i}, 6 - 8 \mathbb{i}, 6 + 8 \mathbb{i}, 8 - 6 \mathbb{i}, 8 + 6 \mathbb{i},$   
 $10, -10 - 5 \mathbb{i}, -10 + 5 \mathbb{i}, -5 - 10 \mathbb{i}, -5 + 10 \mathbb{i},$   
 $5 - 10 \mathbb{i}, 5 + 10 \mathbb{i}, 10 - 5 \mathbb{i}, 10 + 5 \mathbb{i}, -14 - 2 \mathbb{i},$   
 $-14 + 2 \mathbb{i}, -10 - 10 \mathbb{i}, -10 + 10 \mathbb{i}, -2 - 14 \mathbb{i},$   
 $-2 + 14 \mathbb{i}, 2 - 14 \mathbb{i}, 2 + 14 \mathbb{i}, 10 - 10 \mathbb{i}, 10 + 10 \mathbb{i},$   
 $14 - 2 \mathbb{i}, 14 + 2 \mathbb{i}, -15 - 5 \mathbb{i}, -15 + 5 \mathbb{i}, -5 - 15 \mathbb{i},$   
 $-5 + 15 \mathbb{i}, 5 - 15 \mathbb{i}, 5 + 15 \mathbb{i}, 15 - 5 \mathbb{i}, 15 + 5 \mathbb{i},$   
 $-20, -16 - 12 \mathbb{i}, -16 + 12 \mathbb{i}, -12 - 16 \mathbb{i},$   
 $-12 + 16 \mathbb{i}, -20 \mathbb{i}, 20 \mathbb{i}, 12 - 16 \mathbb{i}, 12 + 16 \mathbb{i},$   
 $16 - 12 \mathbb{i}, 16 + 12 \mathbb{i}, 20, -20 - 10 \mathbb{i}, -20 + 10 \mathbb{i},$   
 $-10 - 20 \mathbb{i}, -10 + 20 \mathbb{i}, 10 - 20 \mathbb{i}, 10 + 20 \mathbb{i},$   
 $20 - 10 \mathbb{i}, 20 + 10 \mathbb{i}, -25, -25 \mathbb{i}, 25 \mathbb{i}, 25,$   
 $-30 - 10 \mathbb{i}, -30 + 10 \mathbb{i}, -10 - 30 \mathbb{i}, -10 + 30 \mathbb{i},$   
 $10 - 30 \mathbb{i}, 10 + 30 \mathbb{i}, 30 - 10 \mathbb{i}, 30 + 10 \mathbb{i},$   
 $-25 - 25 \mathbb{i}, -25 + 25 \mathbb{i}, 25 - 25 \mathbb{i}, 25 + 25 \mathbb{i},$   
 $-40 - 20 \mathbb{i}, -40 + 20 \mathbb{i}, -20 - 40 \mathbb{i}, -20 + 40 \mathbb{i},$   
 $20 - 40 \mathbb{i}, 20 + 40 \mathbb{i}, 40 - 20 \mathbb{i}, 40 + 20 \mathbb{i},$   
 $-50, -50 \mathbb{i}, 50 \mathbb{i}, 50, -50 - 50 \mathbb{i}, -50 + 50 \mathbb{i},$   
 $50 - 50 \mathbb{i}, 50 + 50 \mathbb{i}, -100, -100 \mathbb{i}, 100 \mathbb{i}, 100\}$

There are 180 divisors of 100.  
100 is not prime.