

## 5800 Test 2 Study Guide

### HW 6 –

Problems 1 and 2:

Showing that a sequence of functions  $f_n$  converges to a function  $f$  pointwise on some set.

Problems 3 and 4:

Draw a picture of the standard sequence.

Show that the standard sequence converges to  $f$  on  $[a,b]$ .

Problems 5 and 6:

Proofs involving convergence of sequences of functions (pointwise or almost everywhere).

### HW 7 –

Problem 1:

Step functions are in  $L^0$  and  $L^1$ .

Problem 2:

An example of a function that is not in  $L^1$ .

Problems 8 and 9:

Be able to compute the integral of the standard construction.

Use the standard construction to compute the integral of a function in  $L^1$ .

Problem 3 – 7:

Proofs involving  $L^0$  and  $L^1$

Problem 10:

Example of a function in  $L^1(I)$  using rationals and irrationals.

Problem 11:

This is a good example of a function that is in  $L^0$  and we aren't using the standard construction to approximate it.

Misc:

Look at not only using the standard construction, but also any other ways of showing a function is in  $L^0$ . For example problems 10 and 11 and any ones we did in class. Then you have a good example base for  $L^0$  and  $L^1$ .

Problem 12:

Don't worry about this one unless you feel like filling in some of the steps that we skipped in class or if you want more practice with sums of coverings.