Solutions to FE Exam "Dynamics" Review Problems

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Presented here are my solutions to the "Dynamics" review problems that used to be available online, until the end of 2017, on the website for the book: Beer and Johnston, *Vector Mechanics for Engineers, Statics and Dynamics*, Ninth Edition, 2010, at: <u>http://highered.mcgraw-hill.com/sites/0073529400/information_center_view0/</u>. Before these review problems went "Out of Print," I downloaded and collected them in the following "problems.pdf" file: <u>https://www.calstatela.edu/sites/default/files/problems.pdf</u>.

My solutions, which you will find below, are for the review problems that are associated with the following chapters and topics in the above book:

- Chpt. 11: Kinematics of Particles
- Chpt. 12: Kinetics of Particles: Newton's Second Law
- Chpt. 13: Kinetics of Particles: Energy and Momentum Methods
- Chpt. 14: Systems of Particles
- Chpt. 15: Kinematics of Rigid Bodies
- Chpt. 16: Plane Motion of Rigid Bodies: Forces and Accelerations
- Chpt. 17: Plane Motion of Rigid Bodies: Energy and Momentum Methods
- Chpt. 19: Mechanical Vibrations

As I mentioned in class, some of the formerly available online problem statements had errors in them, and some online solutions and answers were wrong! For this reason, I have included in the above mentioned "problems.pdf" file a list of errors and corrections. Although I shared the errors and corrections with McGraw-Hill, the company never made any corrections to its Website.

The formerly available online problems were not numbered; they were identified by chapter numbers only. For this reason, when I downloaded the online problems, I numbered them consecutively in a decimal format, XX.X, where XX refers to the chapter number, and X stands for the sequence number. All the downloaded problems numbered this way are included in the above mentioned "problems.pdf" file under the heading: "Part 1, FE Exam Review, Online Problems and Solutions."

My own solutions, which you will find below, follow the problem numbering scheme I established above. I included sketches in my solutions to allow you to identify more easily the problems to which my solutions apply.

I wish you all the best on your computer-based FE exam!

$$\begin{array}{c|c} \begin{array}{c} (\lambda_{p} + . 11) \\ \hline \\ 11.1 \\ \hline \\ 11.1 \\ \hline \\ 11.1 \\ \hline \\ 11.1 \\ \hline \\ 11.2 \\ \hline \\ 11.3 \\ \hline \\ 11.3 \\ \hline \\ 11.3 \\ \hline \\ 11.3 \\ \hline \\ \\ 11.3 \\ \hline \\ 11.3 \\ \hline \\ \\ 11.3 \\ \hline \\ 11.3 \\ \hline \\ 11.3 \\ \hline \\ 11.3 \\ \hline \\ 11.4 \\ \hline \\$$



INSERT AFTER







 $ZF_{x} = ma$ mgsin 45° = ma $a = (9.8i) \cos 45^\circ = 6.94 \frac{m}{s^2}$ < Ans.



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13.2
Conservation of total
linear momentum:

$$m_{A}\tau_{A} + m_{B}\sigma_{B} = m_{A}\tau_{A} + m_{B}\sigma_{B}^{-1}$$

$$m_{A}\tau_{A} + m_{B}\sigma_{B} = m_{A}\tau_{A}^{-1}$$

$$m_{A}\tau_{A} + m_{B}\sigma_{B} = m_{A}\tau_{A}^{-1}$$

$$m_{A}\tau_{A} + m_{B}\sigma_{B} = m_{A}\tau_{A}^{-1}$$

$$m_{A}\sigma_{A} + m_{B}\sigma_{B} = m_{A}\tau_{A}^{-1}$$

$$m_{A}\sigma_{A} = m_{A$$

$$SUV = 10 \text{ m/s}$$

$$Initial \qquad \text{momentum} \qquad \text{Fat}$$

$$e = \frac{\tau_B' - \tau_A'}{\tau_A' - \tau_B'' \tau_A'} \qquad \text{Collision} \qquad \text{Fat}$$

$$e = \frac{\tau_B' - \tau_A'}{\tau_A' - \tau_B'' \tau_A'} \qquad \text{Impulses} \qquad \text{Fat}$$

$$Conservation of total linear momentum: \qquad \text{mat} \tau_A' + \text{mg} \tau_B'' \qquad \text{mat} \tau_A'' + \text{mg} \tau_B'' \qquad \text{mat} \tau_A' + \text{mg} \tau_B'' \qquad \text{mat} \tau_B'' = 10.2 \text{ m/s} \qquad \text{mat} \tau_B'' = 10.2 \text{ m/s} \qquad \text{mat} \tau_B'' = \frac{(4000)(10.2)}{0.3} = 136 \text{ kN} \qquad \text{Ans}.$$

$$F = \frac{\text{mg} \tau_B'}{\Delta t} = \frac{(4000)(10.2)}{0.3} = 136 \text{ kN} \qquad \text{Ans}.$$

$$F = \frac{\text{mg} \tau_B'}{\Delta t} = \frac{(100)(10.2)}{10^5} = 136 \text{ kN} \qquad \text{Ans}.$$

$$F = \frac{\text{mg} \tau_B'}{\Delta t} = \frac{(100)(10.2)}{10^5} = 136 \text{ kN} \qquad \text{Ans}.$$

$$F = \frac{\text{mg} \tau_B'}{\Delta t} = \frac{(100)(10.2)}{10^5} = 136 \text{ kN} \qquad \text{Ans}.$$

$$F = \frac{\text{mg} \tau_B'}{\Delta t} = \frac{(100)(10.2)}{10^5} = 136 \text{ kN} \qquad \text{Ans}.$$

$$F = \frac{1000}{10^5} = \frac{1000}{10^5} = 126 \text{ kN} \qquad \text{Ans}.$$

$$F = \frac{1000}{10^5} = \frac{1000}{10^5} = 126 \text{ kN} \qquad \text{Ans}.$$

$$F = \frac{1000}{10^5} = \frac{1000}{10^5} = 1200 \text{ m}.$$

$$F = 0.1 \text{ kN/mm} (NEW) = 98.1 \times 10^{-5} \text{ m}$$

$$O = \Delta T + \Delta V_g + \Delta V_e$$

$$O = \frac{1}{1} \text{ m} \tau_{ac}^{2} - \text{mg} (\pi_{ac} - \pi_{ac}) + \frac{1}{2} \text{ k} (\pi_{ac}^{2} - \pi_{ac}^{2})$$

$$\tau_{ac}^{2} = \frac{2}{10} \left[(-10)(9.81)(0.02 - 98.1 \times 10^{-5}) + \frac{1}{10^5}(0.02^{5} - 98.1^{5} \times 10^{-10}) \right]$$

$$\tau_{ac}^{2} = 3.617 \implies \tau_{ac} = 1.902 \text{ m}$$

13.5

13.6

$$\begin{array}{c} 13.7 \qquad \begin{array}{c} 13.7 \qquad \end{array} \end{array} \\ \begin{array}{c} 13.7 \qquad \begin{array}{c} 13.7 \qquad \end{array} \end{array} \\ \begin{array}{c} 13.7 \qquad \begin{array}{c} 13.7 \qquad \end{array} \end{array} \\ \begin{array}{c} 13.7 \qquad \end{array} \end{array} \\ \begin{array}{c} 13.7 \qquad \end{array} \end{array} \\ \begin{array}{c} 13.7 \qquad \end{array} \\ \begin{array}{c} 13.7 \qquad \end{array} \end{array} \\ \begin{array}{c} 13.7 \qquad \end{array} \\ \begin{array}{c} 13.7 \qquad \end{array} \\ \begin{array}{c} 13.7 \qquad \end{array} \end{array} \\ \begin{array}{c} 13.7 \qquad \end{array} \\ \begin{array}{c} 14.1 \quad \begin{array}{c} 13.7 \qquad \end{array} \\ \begin{array}{c} 14.7 \quad \end{array}$$

$$\begin{array}{c} 14.3 \\ m = 5 \ \text{kg} \qquad r = 10 \ \text{i} - 2j + 5 \ \text{k}, m \\ \underline{w} = 3 \ \text{i} + 2j - 5 \ \text{k}, m/s \\ \underline{H}_{o} = r \times m \ v = 5 \\ \left| \begin{array}{c} \frac{i}{2} & \frac{j}{2} & \frac{j}{4} \\ 3 & 2 & -5 \end{array} \right| \\ = 5 \left[\frac{i}{2} (10 - 10) - j (-50 - 15) + \frac{j}{4} (20 + 6) \right] \\ = 325 \ j + 130 \ \text{k}, \ \frac{k_{0} \cdot m^{2}}{s} \\ \frac{M_{0} \cdot m_{1}}{s} \\ \frac{M_{1} \cdot m_{2}}{s} \\ 0 = \frac{1}{2} \ m_{1} \left(\frac{\pi_{1}}{s} \right)^{2} \right] + m_{0} \left[\frac{y_{1}}{2} - 0 \right] \\ \frac{y_{1}}{s} \\ \frac{14.4}{s} \\ \text{See} (7) \ bottom \implies v_{1}^{r} = 4 \ \frac{m_{1}}{s} \\ m_{1} : 0 = \Delta T + \Delta V_{3} \\ 0 = \left[0 - \frac{1}{2} \ m_{1} \left(\frac{\pi_{1}}{s} \right)^{2} \right] + m_{0} \left[\frac{y_{1}}{2} - 0 \right] \\ \frac{y_{1}}{s} \\ \frac{y_{1}}{s} \\ \frac{y_{1}}{s} \\ \frac{14.5}{m_{1}} \\ \frac{m_{1}}{w_{2}} \\ \frac{m_{1}}{s} \\ \frac{m_{2}}{v_{2}} \\ \frac{m_{1}}{w_{2}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{1}}{v_{2}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{1}}{v_{2}} \\ \frac{m_{1}}{w_{2}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{1}}{v_{2}} \\ \frac{m_{1}}{v_{2}} \\ \frac{m_{1}}{v_{2}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{2}}{v_{2}} \\ \frac{m_{2}}{v_{2}} \\ \frac{m_{2}}{v_{2}} \\ \frac{m_{2}}{v_{2}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{2}}{v_{2}} \\ \frac{m_{1}}{v_{2}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{2}}{v_{1}} \\ \frac{m_{2}}{v_{2}} \\ \frac{m_{2}}{v_{$$

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$$B = 5 \frac{rad}{s} V$$

$$B = 10 \frac{rad}{s^2} V$$

$$B = 10 \frac{rad}{s^2} V$$

$$Wsing the ICR of BC:$$

$$W_{Bc} = \frac{v_B}{V^2 o_{,1}}$$

$$W_{Bc} = \frac{w_{AB} AB}{V^2 o_{,1}} = \frac{(5)(.1414)}{V^2 o_{,1}}$$

$$= 5 \frac{rad}{s} G$$

$$v_c = w_{Bc} O_{,1} = 0.5$$

$$v_c = w_{cp} CD$$

$$W_{cp} = \frac{0.5}{0.2} = 2.5 \frac{rad}{s} V$$

(l)

$$\begin{aligned} \underline{a}_{c} &= \underline{a}_{B} + \underline{a}_{c/B} \\ (\underline{a}_{c})_{t} + (\underline{a}_{c})_{n} &= (\underline{a}_{B})_{t} + (\underline{a}_{B})_{n} + (\underline{a}_{c/B})_{t} + (\underline{a}_{c/B})_{n} \quad (I) \\ (\underline{a}_{c})_{n} &= \omega_{cD}^{2} \overline{CD} = (2.5)^{2} (0.20) = 1.25 \text{ m/s}^{2} \\ (\underline{a}_{B})_{t} &= \omega_{AB} \ \overline{AB} = (10)(0.1414) = 1.414 \text{ m/s}^{2} \\ (\underline{a}_{B})_{n} &= \omega_{AB}^{2} \ \overline{AB} = (5)^{2} (0.1414) = 3.535 \text{ m/s}^{2} \\ (\underline{a}_{c/B})_{n} &= \omega_{Bc}^{2} \ \overline{BC} = (5)^{2} (0.11) = 2.5 \text{ m/s}^{2} \end{aligned}$$
Vector diagram of (I):

$$(a_{c/B})_{t} = \frac{(a_{c})_{t}}{(a_{c/B})_{n}} = \frac{(a_{c})_{t}}{\sqrt{z}} - \frac{(a_{B})_{t}}{\sqrt{z}} + (a_{c})_{B})_{n}$$

$$= \frac{3.535}{\sqrt{z}} - \frac{1.414}{\sqrt{z}} + 2.5$$

$$= 4 m/s^{2}$$

$$(a_{c/B})_{n} = \frac{3}{\sqrt{z}} - \frac{1.414}{\sqrt{z}} + 2.5$$

$$= 4 m/s^{2}$$

$$Ans$$

15.6

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$$16.1 \qquad FBD \qquad KD \qquad (i)$$

$$16.1 \qquad FBD \qquad FBD \qquad KD \qquad (i)$$

$$16.1 \qquad FBD \qquad FBD \qquad FD \qquad (i)$$

$$16.1 \qquad FBD \qquad FD \qquad (i)$$

$$16.1 \qquad FD \qquad FD \qquad FD \qquad FD \qquad FD \qquad (i)$$

$$(i) \qquad FD \qquad (i) \qquad FD \qquad (i)$$

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$$(i) \qquad (i) \qquad (i)$$









Conservation of angular momentum about A: $m_{s}vL = m_{s}v'L + I_{r}\omega_{r}' + m_{r}v_{r}'\frac{L}{2}$ $m_{s}vL = m_{s}v'L + \frac{1}{12}m_{r}L^{2}\frac{2v_{r}'}{L} + m_{r}v_{r}'\frac{L}{2}$ $m_{s}vL = m_{s}v'A + \frac{2}{3}m_{r}v_{r}'Y$ () $e = \frac{2v_{r}' - v'}{v}$ (2) (1)(10) = (1)v' + \frac{2}{3}(10)v_{r}' (3) (2) $(0.7)(10) = -v' + 2v_{r}'$ (4) (3) $-\frac{10}{3}x$ (0) $(-(7)(\frac{10}{3}) = (1 + \frac{10}{3})v'$ $v' = -3.08 \frac{m}{5}$ (Ans.

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$$\frac{3}{2}m\ddot{x} + kx = 0$$

$$\omega_{n} = \sqrt{\frac{4}{3}m} = \sqrt{\frac{850}{3}lo} = 7.53 \frac{md}{5}$$

$$x = 0.02 \cos(\omega_{n} t)$$

$$\dot{x} = 0.02 \omega_{n} (-\sin(\omega_{n} t))$$

$$|\dot{x}|_{max} = 0.02 \omega_{n} = 0.151 \frac{m}{5} \qquad Ans.$$

$$19.4 \quad Above \ figure \qquad \omega_{n} = \frac{2\pi}{2} \implies 2 = 0.8355 \qquad Ans.$$

$$19.5 \quad Figure \ on \ tep \ of \ page \ (B)$$

$$x = 0.03 \omega_{n} \sin(\omega_{n} t)$$

$$|\dot{x}|_{max} = 0.03 \omega_{n} = 0.346 \ mfs \qquad Ans.$$

$$19.6 \qquad \dot{x} = -0.03 \omega_{n}^{*} \cos(\omega_{n} t)$$

$$|\ddot{x}|_{max} = 0.03 \omega_{n}^{*} = 4 \ m/s^{*} \qquad Ans.$$