

# Math 5680

## Homework # 6

### Applications of the residue theorem

1. Evaluate the integral  $\int_0^{2\pi} \frac{d\theta}{2 - \sin(\theta)}$

2. Evaluate the integral  $\int_0^{2\pi} \frac{\cos(3\theta)}{5 - 4\cos(\theta)} d\theta$

[Hint: You might need Mathematica or Wolfram Alpha to calculate a second derivative at one point in the derivation.]

3. Evaluate the integral  $\int_0^{\infty} \frac{dx}{1 + x^6} dx$

4. Evaluate the integral  $\int_0^{\infty} \frac{1 + x^2}{1 + x^4} dx$

5. Evaluate the integral  $\int_{-\infty}^{\infty} \frac{x \sin(x)}{x^4 + 1} dx$