

**Definitions**

$$g := 32.2 \frac{\text{ft}}{\text{s}^2} \quad \text{slug} := \frac{\text{lb}\cdot\text{s}^2}{\text{ft}}$$

**Drum**

$$\begin{aligned} W_d &:= 30 \text{ lb} & m_d &:= \frac{W_d}{g} & m_d &= 0.932 \text{ slug} \\ r &:= 1.5 \text{ ft} & M &:= 120 \text{ lb}\cdot\text{ft} \\ k_0 &:= 0.8 \text{ ft} & I_0 &:= m_d \cdot k_0^2 & I_0 &= 0.596 \text{ slug}\cdot\text{ft}^2 \end{aligned}$$

**Crate**

$$W_A := 15 \text{ lb} \quad m_A := \frac{W_A}{g} \quad m_A = 0.466 \text{ slug}$$

**Motion**

$$v_1 := 0 \cdot \frac{\text{ft}}{\text{s}} \quad \text{when} \quad s_1 := 0 \cdot \text{ft}$$

Find  $v_2$  when  $s_2 := 4 \cdot \text{ft}$

$$U_{1>2} := \Delta T + \Delta V_g$$

$$U_{1>2} := M \cdot \left( \frac{s_2 - s_1}{r} \right) \quad U_{1>2} = 320 \cdot \text{ft}\cdot\text{lb}$$

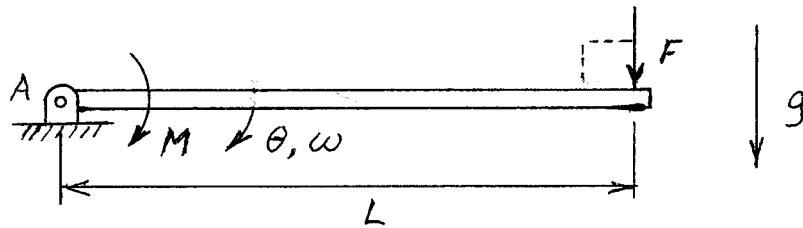
$$\Delta T := \frac{1}{2} \cdot I_0 \cdot \left( \frac{v_2}{r} \right)^2 + \frac{1}{2} \cdot m_A \cdot v_2^2$$

$$\Delta V_g := W_A \cdot (s_2 - s_1) \quad \Delta V_g = 60 \cdot \text{ft}\cdot\text{lb}$$

$$v_2 := \sqrt{\frac{U_{1>2} - \Delta V_g}{\frac{1}{2} \cdot \left( \frac{I_0}{r^2} + m_A \right)}}$$

$$v_2 = 26.7 \cdot \frac{\text{ft}}{\text{s}} \quad \text{Ans.}$$

Problem 18.16, p. 455



$$\text{Definition} \quad g := 9.81 \cdot \frac{\text{m}}{\text{s}^2}$$

$$\text{Rod} \quad m_r := 4 \cdot \text{kg} \quad L := 3 \cdot \text{m} \quad I_A := \frac{1}{3} \cdot m_r \cdot L^2 \quad I_A = 12 \text{ m}^2 \cdot \text{kg}$$

$$\text{Applied couple moment and force} \quad M := 40 \cdot \text{N} \cdot \text{m} \quad F := 15 \cdot \text{N}$$

$$\text{Motion} \quad \omega_1 := 6 \cdot \frac{\text{rad}}{\text{s}} \quad \text{when} \quad \theta_1 := 0 \cdot \text{rad}$$

$$\text{Find } \omega_2 \quad \text{when} \quad \theta_2 := \frac{\pi}{2} \cdot \text{rad}$$

$$U_{1>2} := \Delta T + \Delta V_g$$

$$U_{1>2} := M \cdot (\theta_2 - \theta_1) + F \cdot L \cdot (\theta_2 - \theta_1) \quad U_{1>2} = 133.5 \text{ J}$$

$$\Delta T := \frac{1}{2} \cdot I_A \cdot (\omega_2^2 - \omega_1^2)$$

$$\Delta V_g := -m_r \cdot g \cdot \frac{L}{2} \quad \Delta V_g = -58.86 \text{ J}$$

$$\omega_2 := \sqrt{\frac{U_{1>2} - \Delta V_g + \frac{1}{2} \cdot I_A \cdot \omega_1^2}{\frac{1}{2} \cdot I_A}} \quad \omega_2 = 8.25 \cdot \frac{\text{rad}}{\text{s}} \quad \text{Ans.}$$

Problem 18.17

$$\text{Find } \omega_2 \quad \text{when} \quad \theta_2 := 2 \cdot \pi \cdot \text{rad}$$

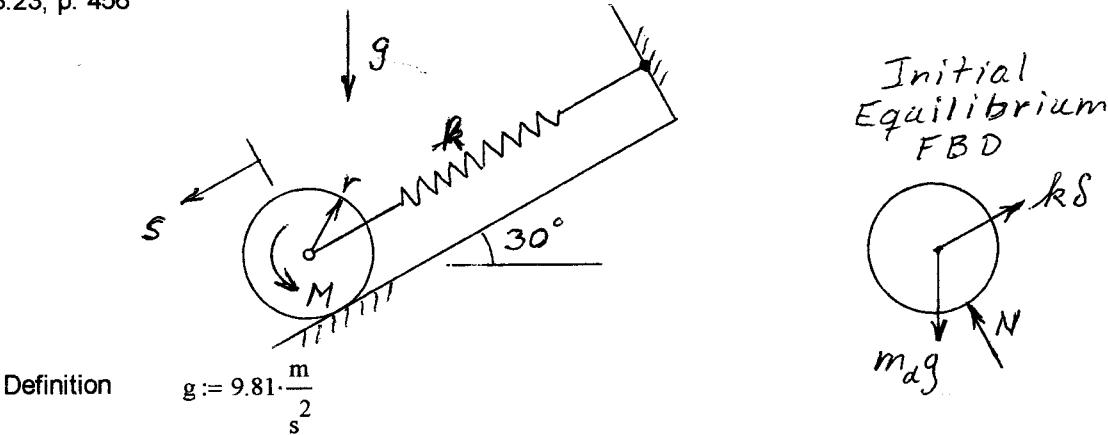
$$U_{1>2} := \Delta T + \Delta V_g$$

$$U_{1>2} := M \cdot (\theta_2 - \theta_1) + F \cdot L \cdot (\theta_2 - \theta_1) \quad U_{1>2} = 534.1 \text{ J}$$

$$\Delta T := \frac{1}{2} \cdot I_A \cdot (\omega_2^2 - \omega_1^2)$$

$$\Delta V_g := 0$$

$$\omega_2 := \sqrt{\frac{U_{1>2} - \Delta V_g + \frac{1}{2} \cdot I_A \cdot \omega_1^2}{\frac{1}{2} \cdot I_A}} \quad \omega_2 = 11.18 \cdot \frac{\text{rad}}{\text{s}} \quad \text{Ans.}$$



Definition  $g := 9.81 \cdot \frac{\text{m}}{\text{s}^2}$

Disk

$$m_d := 20 \cdot \text{kg} \quad r := 0.2 \cdot \text{m} \quad M := 30 \cdot \text{N}\cdot\text{m}$$

Spring

$$k := 150 \cdot \frac{\text{N}}{\text{m}}$$

Motion

$$v_1 := 0 \cdot \frac{\text{m}}{\text{s}} \quad \text{when} \quad s_1 := 0 \quad \text{and disk is held in equilibrium by spring.}$$

Let  $\delta$  be the initial elongation of the spring at equilibrium.

$$\delta := \frac{m_d \cdot g \cdot \sin(30\text{-deg})}{k} \quad \delta = 0.654 \text{ m}$$

$$\text{Find } s_2 \quad \text{when} \quad v_2 := 0 \cdot \frac{\text{m}}{\text{s}}$$

$$U_{1>2} := \Delta T + \Delta V_g + \Delta V_e$$

$$U_{1>2} := M \cdot \left( \frac{s_2 - s_1}{r} \right)$$

$$\Delta T := 0 \cdot \text{J}$$

$$\Delta V_g := -m_d \cdot g \cdot (s_2 - s_1) \cdot \sin(30\text{-deg})$$

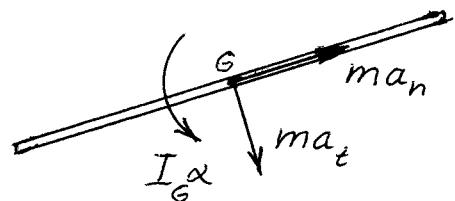
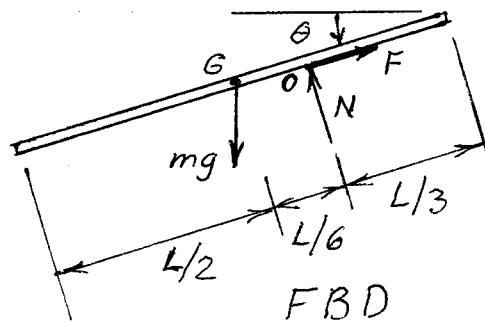
$$\Delta V_e := \frac{1}{2} \cdot k \cdot [(s_2 + \delta)^2 - \delta^2] \quad \Delta V_e := \frac{1}{2} \cdot k \cdot [s_2 \cdot (2 \cdot \delta + s_2)]$$

$$M \cdot \left( \frac{s_2}{r} \right) := -m_d \cdot g \cdot (s_2) \cdot \sin(30\text{-deg}) + \frac{1}{2} \cdot k \cdot [s_2 \cdot (2 \cdot \delta + s_2)]$$

$$s_2 := \frac{M \cdot \left( \frac{1}{r} \right) + m_d \cdot g \cdot (1) \cdot \sin(30\text{-deg}) - k \cdot \delta}{\frac{1}{2} \cdot k} \quad s_2 = 2 \text{ m} \quad \text{Ans.}$$

Problem 18.27, p. 457

Definitions



KD

Bar mass: m

Bar length: L

Gravity: g

Coeff. of static friction:  $\mu_s := 0.3$

Motion:

$$\omega_1 := 0 \frac{\text{rad}}{\text{s}} \quad \text{when} \quad \theta_1 := 0 \cdot \text{rad}$$

Find  $\theta_2$  when  $F := \mu_s \cdot N$  and bar begins to slip.

Equations of motion

$$\Sigma F_n := m \cdot a_n \quad F - m \cdot g \cdot \sin(\theta) := m \cdot a_n \quad a_n := \frac{L}{6} \cdot \omega^2$$

$$F := m \cdot g \cdot \sin(\theta) + m \cdot \left( \frac{L}{6} \cdot \omega^2 \right)$$

$$\Sigma F_t := m \cdot a_t \quad -N + m \cdot g \cdot \cos(\theta) := m \cdot a_t \quad a_t := \alpha \cdot \frac{L}{6}$$

$$N := m \cdot g \cdot \cos(\theta) - m \cdot \left( \alpha \cdot \frac{L}{6} \right)$$

$$\Sigma M_O := I_O \cdot \alpha \quad m \cdot g \cdot \cos(\theta) \cdot \frac{L}{6} := I_O \cdot \alpha$$

$$I_O := \frac{1}{12} \cdot m \cdot L^2 + m \cdot \left( \frac{L}{2} - \frac{L}{3} \right)^2 \quad I_O := \frac{1}{9} \cdot m \cdot L^2$$

$$\alpha := \frac{m \cdot g \cdot \cos(\theta) \cdot \frac{L}{6}}{\frac{1}{9} \cdot m \cdot L^2}$$

$$\alpha := \frac{3 \cdot g \cdot \cos(\theta)}{2 \cdot L}$$

Find  $\omega^2$

$$0 := \Delta T + \Delta V g$$

$$0 := \frac{1}{2} \cdot I_0 \cdot \omega^2 - m \cdot g \cdot \frac{L}{6} \cdot \sin(\theta) \quad \omega^2 := \frac{m \cdot g \cdot \frac{L}{6} \cdot \sin(\theta)}{\frac{1}{2} \left( \frac{1}{9} \cdot m \cdot L^2 \right)}$$

$$\omega^2 := \frac{3 \cdot g \cdot \sin(\theta)}{L}$$

Substitute the expressions for  $\omega^2$  and  $\alpha$  in the equations for F and N, respectively.

$$F := m \cdot g \cdot \sin(\theta) + m \cdot \left( \frac{L}{6} \cdot \frac{3 \cdot g \cdot \sin(\theta)}{L} \right) \quad F := \frac{3 \cdot g \cdot m \cdot \sin(\theta)}{2}$$

$$N := m \cdot g \cdot \cos(\theta) - m \cdot \left( \frac{3 \cdot g \cdot \cos(\theta)}{2 \cdot L} \cdot \frac{L}{6} \right) \quad N := \frac{3 \cdot g \cdot m \cdot \cos(\theta)}{4}$$

Develop  $F := \mu_s \cdot N$  and simplify.

$$\frac{3 \cdot g \cdot m \cdot \sin(\theta)}{2} := 0.3 \cdot \frac{3 \cdot g \cdot m \cdot \cos(\theta)}{4}$$

$$\tan(\theta) := 0.3 \cdot \frac{\frac{3 \cdot g \cdot m}{4}}{\frac{3 \cdot g \cdot m}{2}}$$

$$\tan(\theta) := 0.15$$

$$\theta := \text{atan}(0.15) \quad \theta = 8.53 \cdot \text{deg} \quad <----- \text{Ans.}$$