

Implementing an Approximate Probabilistic Algorithm for Error Recovery in Concurrent Processing Systems

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Overview

- Problem Statement
- Recovery Algorithms
- Previous Work
- Implementation Issues
- Approximate Probabilistic Algorithm
- Simulation
- Comparison of Performance
- Conclusion

Problem Statement

- Design of a reliable concurrent processing system
- Transient errors detected by acceptance tests (AT) with a delay
- Consistent system states established using (global) checkpoints
- Error recovery is attempted by rolling back to previously established checkpoint and restarting the system
- What is the best method for rollback recovery?

Recovery Algorithms

➤ Iterative Algorithm

- Rolls back one checkpoint (CP) at a time, starting from most recent one
- Recovery (if possible) is achieved from the CP just prior to failure

➤ Probabilistic Algorithm

- Based on distribution of latency times
- Selects CP for recovery by comparing pairs of checkpoints for smaller expected cost of recovery

Previous Work

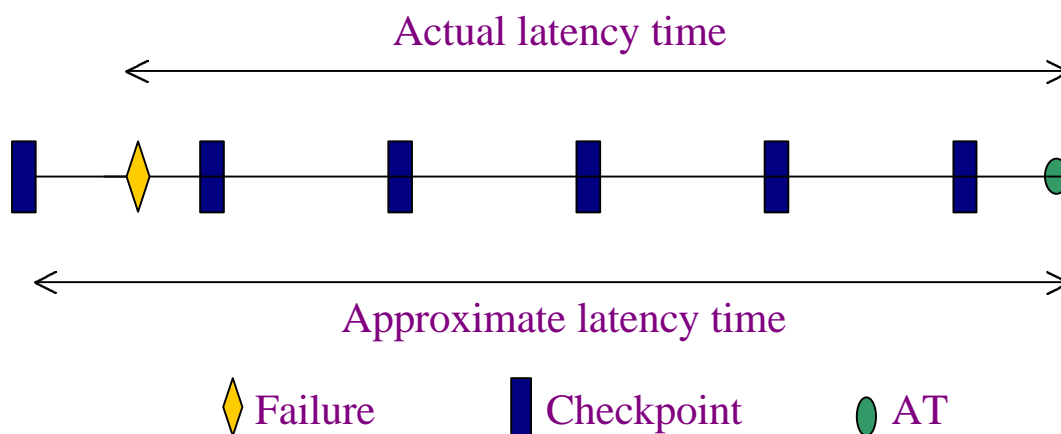
- Simulation of 4 concurrent processes
- Waiting times between events are independent exponential random variables
- Ranges for average times between
 - inter-connections: .25 - 1 (hours)
 - failures: 10 - 40 (hours)
 - acceptance tests: 1 - 2 (hours)
- Result: Probabilistic Algorithm better if checkpoint interval length $<$ median of latency time distribution (= .45)

Implementation Issues

- Can't measure exact latency times (to get empirical distribution function)
- Theoretical derivation of latency distribution difficult due to dependencies introduced through inter-connections
- Solution: Approximate Probabilistic Algorithm

Approximate Probabilistic Algorithm (APA)

- Use iterative method to measure approximate latency times



- Compute empirical distribution function of approximate latency times
- Switch to probabilistic method based on this empirical distribution function

Approximate Probabilistic Algorithm (APA)

- APA works for all distributions and allows for dependent events as well
- No parameter estimation needed (as would be necessary if one would be able to derive the theoretical distribution of latency times)
- Easy to implement
- Parameters for Implementation
 - N = number of data points collected using iterative algorithm
 - Length of checkpoint interval (=: error interval) during data collection phase

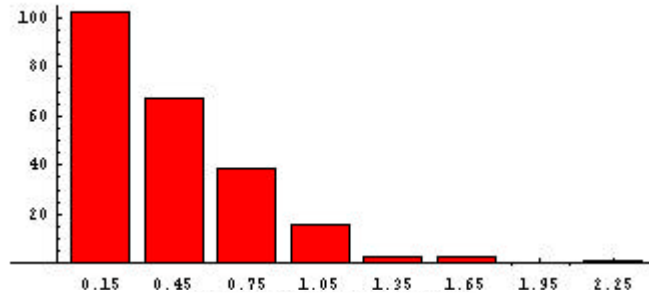
Simulation

- Two phases
 - data collection
 - performance comparison

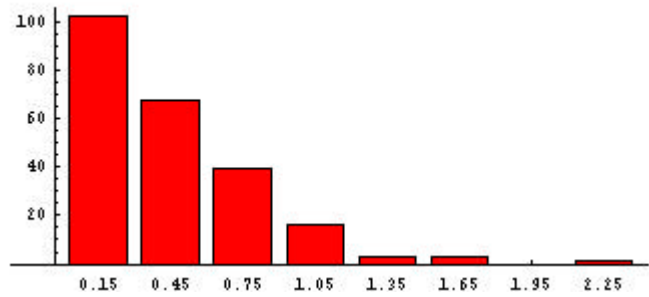
- Phase I
 - 10 simulations, each up to 100 hours
 - 231 detected failures
 - exact and approximate latency times measured for error interval lengths 0.1, 0.15, 0.2, and 0.25

➤ Latency Time Distributions

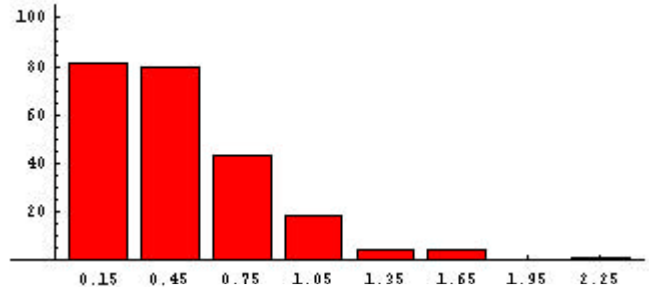
exact



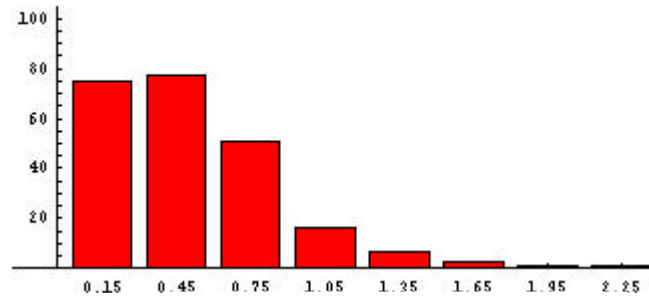
0.1



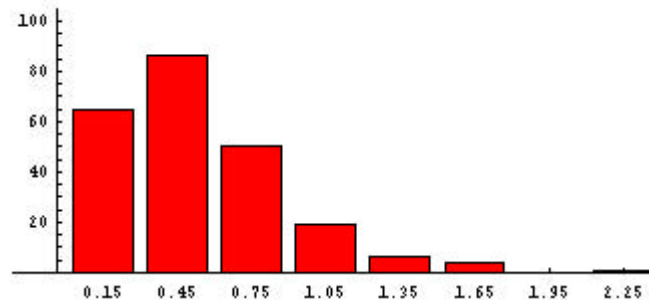
0.15



0.2



0.25



Simulation (Phase II)

- 30 simulations (up to time 100) for each combination of
 - CP interval length $C = 0.1, 0.15, \dots, 0.45$
 - Recovery level 90% and 95%
 - $N = 25, 50, 75, 100, 150$ and 200
- Compute average cost for each case
- Performance measure: Cost of APA as percentage of cost incurred with iterative algorithm

Comparison of Performance

Exact Probabilistic

		<i>N</i>					
		25	50	75	100	150	200
<i>C</i>	0.10	56.5	50.5	46.7	49.6	54.2	49.1
	0.15	71.7	65.5	63.8	64.0	65.7	63.4
	0.20	82.5	75.5	72.5	74.2	73.5	76.2
	0.25	88.8	83.1	82.4	81.3	80.7	80.4
	0.30	94.4	88.9	87.2	86.5	89.1	87.6
	0.35	93.6	95.8	95.2	91.7	94.3	96.5
	0.40	97.0	97.9	94.7	99.3	97.6	96.7
	0.45	99.2	99.2	97.3	99.2	96.9	97.1

≤59.99
 60 - 69.99
 70 -79.99
 80 - 89.99
 >100.5

- probabilistic method better
- for $C = .40$ and $.45$, methods almost identical
- if $N = 25$ is disregarded, get nice efficiency brackets

Comparison of Performance

Exact Probabilistic

		<i>N</i>					
		25	50	75	100	150	200
<i>C</i>	0.10	56.5	50.5	46.7	49.6	54.2	49.1
	0.15	71.7	65.5	63.8	64.0	65.7	63.4
	0.20	82.5	75.5	72.5	74.2	73.5	76.2
	0.25	88.8	83.1	82.4	81.3	80.7	80.4
	0.30	94.4	88.9	87.2	86.5	89.1	87.6
	0.35	93.6	95.8	95.2	91.7	94.3	96.5
	0.40	97.0	97.9	94.7	99.3	97.6	96.7
	0.45	99.2	99.2	97.3	99.2	96.9	97.1

Error Interval 0.1

		<i>N</i>					
		25	50	75	100	150	200
<i>C</i>	0.1	54.9	53.3	53.1	52.1	57.2	51.6
	0.15	79.6	69.8	65.1	67.2	69.7	66.9
	0.2	85.2	76.6	72.8	78.4	76.1	75.8
	0.25	93.6	80.8	85.1	88.9	84.3	81.7
	0.3	97.5	97.4	87.6	87.1	98.8	94.0
	0.35	100.8	95.1	94.4	97.7	93.7	93.5
	0.4	99.7	95.6	95.7	94.6	95.9	96.5
	0.45	100.7	108.9	99.1	99.5	107.4	109.6

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Comparison of Performance

Exact Probabilistic

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<i>C</i>	0.10	56.5	50.5	46.7	49.6	54.2	49.1
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	0.25	88.8	83.1	82.4	81.3	80.7	80.4
	0.30	94.4	88.9	87.2	86.5	89.1	87.6
	0.35	93.6	95.8	95.2	91.7	94.3	96.5
	0.40	97.0	97.9	94.7	99.3	97.6	96.7
	0.45	99.2	99.2	97.3	99.2	96.9	97.1

Error Interval 0.15

		<i>N</i>					
		25	50	75	100	150	200
<i>C</i>	0.1	60.5	50.6	50.3	52.0	57.1	51.6
	0.15	79.6	68.1	64.9	65.3	70.9	67.8
	0.2	87.7	77.0	72.9	82.1	80.2	76.1
	0.25	95.9	83.9	85.5	89.0	86.8	82.5
	0.3	100.6	91.4	88.0	87.9	99.2	94.1
	0.35	102.6	96.0	96.4	94.0	94.9	95.3
	0.4	102.6	95.7	96.5	95.7	96.1	97.0
	0.45	107.0	97.9	100.0	99.6	109.1	110.2

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Comparison of Performance

Exact Probabilistic

		<i>N</i>					
		25	50	75	100	150	200
<i>C</i>	0.10	56.5	50.5	46.7	49.6	54.2	49.1
	0.15	71.7	65.5	63.8	64.0	65.7	63.4
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	0.25	88.8	83.1	82.4	81.3	80.7	80.4
	0.30	94.4	88.9	87.2	86.5	89.1	87.6
	0.35	93.6	95.8	95.2	91.7	94.3	96.5
	0.40	97.0	97.9	94.7	99.3	97.6	96.7
	0.45	99.2	99.2	97.3	99.2	96.9	97.1

Error Interval 0.2

		<i>N</i>					
		25	50	75	100	150	200
<i>C</i>	0.1	62.0	52.3	52.4	57.4	58.1	52.7
	0.15	81.1	70.8	67.5	70.1	71.1	68.2
	0.2	90.5	77.2	75.0	83.5	78.5	76.1
	0.25	94.0	83.8	84.9	89.6	86.4	82.6
	0.3	102.0	97.9	88.0	88.5	98.1	93.3
	0.35	103.9	92.2	97.7	99.3	95.2	94.0
	0.4	101.7	93.7	96.3	93.9	96.5	97.4
	0.45	101.8	109.4	100.1	101.4	109.5	110.1

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Comparison of Performance

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	0.15	71.7	65.5	63.8	64.0	65.7	63.4
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	0.25	88.8	83.1	82.4	81.3	80.7	80.4
	0.30	94.4	88.9	87.2	86.5	89.1	87.6
	0.35	93.6	95.8	95.2	91.7	94.3	96.5
	0.40	97.0	97.9	94.7	99.3	97.6	96.7
	0.45	99.2	99.2	97.3	99.2	96.9	97.1

Error Interval 0.25

		<i>N</i>					
		25	50	75	100	150	200
<i>C</i>	0.1	65.5	58.5	52.5	54.0	62.6	53.3
	0.15	88.9	77.5	68.5	68.7	75.8	69.9
	0.2	98.9	85.1	75.1	83.5	85.1	78.2
	0.25	100.9	89.4	89.1	89.2	93.2	83.5
	0.3	108.5	97.6	92.2	88.5	101.3	94.1
	0.35	107.1	100.1	98.2	99.7	94.4	93.2
	0.4	109.3	94.3	96.6	94.4	96.1	97.2
	0.45	107.3	108.6	99.7	100.1	109.6	109.6

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Conclusion

- ◆ APA performs very similar to "exact" probabilistic method for error interval length 0.1 and $N > 25$
 - At least 40% for $C = 0.1$
 - At least 30% for $C = 0.15$
 - At least 20% for $C = 0.2$
 - At least 10% for $C = 0.25$

- ◆ For error interval lengths 0.15 and 0.2, APA achieves comparable efficiency brackets

- ◆ APA universally applicable, independent of assumptions on waiting times between events

Future Work

➤ Simulation

- uniform selection of data points for all error intervals
- other distributions

➤ Theoretical results

- number of data points necessary as function of error interval length

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